Exponent Rules

$$y = b^x$$

When x = 0, y = 1: $b^0 = 1$ $10^0 = 1$ $28^0 = 1$

When x = 1, y = b: $b^1 = b$ $8^1 = 8$ $51^1 = 51$

When a base to an exponent is raised to another exponent, keep the base the same and multiply the exponents:

$$(b^x)^a = b^{x^*a}$$
 $(2^3)^2 = 2^{3^*2} = 2^6$ Think of $(2^3)^2 = (2^{\bullet}2^{\bullet}2)(2^{\bullet}2^{\bullet}2) = 2^6$

When two numbers with the same base are multiplied, keep the base the same and add the exponents:

$$b^x \bullet b^a = b^{x+a}$$
 $3^2 \bullet 3^4 = 3^{2+4} = 3^6$ Think of $3^2 \bullet 3^4 = (3\bullet 3)(3\bullet 3\bullet 3\bullet 3) = 3^6$

When two numbers with the same base are divided, keep the base the same and subtract the exponents:

$$\frac{b^{x}}{b^{a}} = b^{x-a} \qquad \qquad \frac{4^{5}}{4^{2}} = 4^{5-2} = 4^{3} \qquad \qquad \text{Think of } \frac{4^{5}}{4^{2}} = \frac{4 \cdot 4 \cdot 4 \cdot 4 \cdot 4}{4 \cdot 4} = 4^{3}$$

*Note: If the exponent in the denominator is larger, the result will be a number with a negative exponent.

When a number has a negative exponent, put the number in the denominator of a fraction with 1 on top and change the sign of the exponent to positive:

$$b^{-x} = \frac{1}{b^x}$$
 $7^{-3} = \frac{1}{7^3}$

*Note: If the number with the negative exponent is connected to another number, combine the fraction and the other number:

$$g^{a}b^{-x} = g^{a} \cdot \frac{1}{b^{x}} = \frac{g^{a}}{b^{x}}$$
 $5x^{-2} = 5\left(\frac{1}{x^{2}}\right) = \frac{5}{x^{2}}$ $5^{-4}6^{3} = \frac{1}{5^{4}} \cdot 6^{3} = \frac{6^{3}}{5^{4}}$

Square roots are a form of exponents; the square root of a number is that number to the

$$\frac{1}{2}$$
 power: $\sqrt{b} = b^{\frac{1}{2}}$ $\sqrt{8} = 8^{\frac{1}{2}}$ $\frac{1}{\sqrt{12}} = \frac{1}{12^{\frac{1}{2}}} = 12^{-\frac{1}{2}}$