

# Sample document using L<sup>A</sup>T<sub>E</sub>X

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Linear algebra is a **pivotal** tool in 100% of mathematics. A couple applications of linear algebra include:

1. Quantum mechanics
2. Web search engine algorithms

An  $m \times n$  real-valued matrix  $M$  can be viewed as a function from  $\mathbb{R}^n$  to  $\mathbb{R}^m$ . In this context, we call  $M$  a *matrix function*. For example, take  $m = 2$  and  $n = 10$ . If  $x \in \mathbb{R}^{10}$ ,  $y = Mx$  is a vector in  $\mathbb{R}^2$ . Similar statements carry over when working over  $\mathbb{N}$ ,  $\mathbb{Z}$ ,  $\mathbb{Q}$ , or  $\mathbb{C}$ . (There is a feudal war over whether  $\mathbb{N}$  should be  $\{n \in \mathbb{Z} : n \geq 0\}$  or  $\{n \in \mathbb{Z} : n > 0\}$ .)

Let  $D \subseteq X$ . Recall that a function  $f : D \rightarrow Y$  between Banach spaces has a limit  $L$  at  $x_0 \in X$  if  $\forall \epsilon > 0, \exists \delta$  such that  $|x - x_0| < \delta \Rightarrow |f(x) - L| < \epsilon$ . In this case, we write

$$\lim_{x \rightarrow x_0} f(x) = L$$

A function  $f$  is continuous at  $x_0 \in X$  if  $f$  is defined at  $x_0$  and the limit of  $f$  at  $x_0$  is  $f(x_0)$ .

**Theorem 0.1.** *An  $m \times n$  matrix function  $M$  is continuous at all  $x_0 \in \mathbb{R}^n$ .*

*Proof.* Obvious. □

## Sums, integrals, and derivatives

Now, we move on to some harder analysis.

$$\sum_{n=1}^{\infty} \frac{1}{n^2} = \frac{\pi^2}{6} \tag{1}$$

The statement of (1) is known as Basel's problem. It is well-known that

$$\int_{-1}^1 x^3 dx = 0$$

Table 1: Trigonometric values

$\theta$	$\cos \theta$	$\sin \theta$
0	1	0
$\pi/4$	$\sqrt{2}/2$	$\sqrt{2}/2$
$\pi/2$	0	1
$\pi$	-1	0

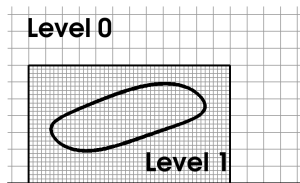


Figure 1: This figure shows an example of adaptive mesh refinement (amr).

Note, however, that if  $g(x) = \sin x$ , then  $\frac{d}{dx}g(x) = \cos(x)$ . This is also sometimes denoted  $\frac{dg}{dx}$  or  $g'(x)$ . As an exercise<sup>1</sup>, compute  $\frac{d}{dx}[\ln(3^{\sec^9 x}) - x^2 e \log_{11} x]$ .

## Tables and figures

Sometimes data needs to be displayed in a table or figure. A good example may be trigonometric data. See Table . Figures are entered with the `includegraphics` command. A figure showing an AMR setup can be seen in Figure . Note:  $\LaTeX$  decides where to put figures and tables.

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<sup>1</sup>Hint, use the Chain Rule!